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Flavored gauge mediation in the Peccei-Quinn NMSSM

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ABSTRACT: We investigate a particular version of the Peccei-Quinn (PQ) NMSSM characterized by an economical and rigidly hierarchical flavor structure and based on flavored gauge mediation and on some considerations inspired by string theory GUTs. In this way we can express the Lagrangian of the PQ NMSSM through very few parameters. The obtained model is studied numerically and confronted with the most relevant phenomenological constraints. We show that typical spectra are for the most part too heavy to be significantly probed at the LHC, but regions of the parameter space exist yielding signatures that might possibly be observed during Run II. We also calculate the fine tuning of the model. We show that, in spite of the appearance of large scales in the superpotential and soft terms, it does not exceed the tuning present in the MSSM for equivalent spectra, which is of the order of 10^4 .

KEYWORDS: Supersymmetry Phenomenology

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1 Introduction

Low scale supersymmetry (SUSY) is still a good candidate for physics beyond the Standard Model (SM) despite a discouraging lack of positive signals in the first run of the LHC. In its unconstrained version the Minimal Supersymmetric Standard Model (MSSM) does not provide a solution to the origin of the flavor structure of the Yukawa couplings, but hierarchical textures are typical of many UV completions, starting from the seminal paper of Froggatt and Nielsen [1], up to more recent developments in F-theory Grand Unified Theories (GUTs), see [2–8] for some early papers. Interestingly, F-theory GUTs provide a natural connection to SUSY breaking, as the visible chiral matter as well as the messengers responsible for conveying the breaking to the visible sector originate from the same D7-brane intersection [6]. A consequence of this fact is the requirement that matter and messengers share common Yukawa couplings.

From the phenomenological point of view, a connection between flavor and SUSY breaking has been developed in models with flavored gauge mediation [9–12], a branch of gauge mediated SUSY breaking (GMSB) [13–19] that links the flavor and messenger sectors of the MSSM. Along these lines, one of us recently proposed [20] a very economical model that successfully incorporates the advantages of Froggatt-Nielsen-like hierarchical Yukawa structures into the GMSB messenger sector.

In [20], all the soft terms depend on one extra parameter, h_3 , which is the coupling between the messenger in the **5** representation of SU(5) and chiral matter. Through well known mixing effects, the extra coupling can also produce a large third-generation soft trilinear term, A_t , which can be used to enhance the radiative corrections to the Higgs mass. A phenomenological analysis of the low-energy limit of this minimal model in the MSSM was presented in [21]. It was shown that, despite quite restrictive constraints on the nature of the matter-messenger couplings, which arise from the flavor structure, it is easy to find regions of the parameter space characterized by particle spectra consistent with the bounds from direct searches for squarks and gluinos at the LHC, and with the measured value of the Higgs boson mass, $m_h \simeq 125 \text{ GeV}$, as well as a number of constraints from flavor-changing neutral current (FCNC) in low-energy processes.

However, the matter/messenger system of ref. [20] is fully consistent with hierarchical flavor structures when the ratio of the Higgs doublets' vacuum expectation values (vev's), $\tan\beta$, is of the order of a few and not larger. As is well known, in the MSSM small values of $\tan\beta$ reduce the size of the tree-level Higgs mass, which therefore requires substantial radiative corrections that imply large soft masses and a consequently high level of fine tuning. Thus, in this paper we analyze whether it is possible to obtain a low-energy limit of the model presented in [20] in the Next-to-Minimal Supersymmetric Standard Model (NMSSM). As is well known, this is achieved by introducing one additional gauge singlet chiral field, S , that couples to the Higgs sector in the superpotential. Because the tree-level value of the Higgs mass for low $\tan\beta$ values can be easily made larger than in the MSSM, the NMSSM seems to be a more natural choice as a low-energy effective theory originating from the model in [20].

In particular, we investigate here the Peccei-Quinn (PQ) version of the NMSSM, which is characterized by the vanishing of the S^3 coupling, $\kappa = 0$ [22–28]. We will build the PQ NMSSM effective action based on arguments from its possible UV completion. It is interesting that similar models appeared in F-theory constructions [6], so that we will often invoke F-theoretic arguments to justify our assumptions.

The purpose of the paper is twofold. We construct a version of the PQ NMSSM, based on a string inspired UV completion and on flavored GMSB, which yields a very predictive framework. The effective action is defined by just a handful of free parameters and we show that the obtained spectra are consistent with the basic phenomenological constraints, although we also show that they are for the most part too heavy to be significantly explored at the LHC.

We further show that the PQ NMSSM analyzed here requires the unavoidable introduction of nonstandard tadpole superpotential and Lagrangian terms, which are linear in the S field, and terms quadratic in S as well, all of them characterized by typical scales that are by orders of magnitude higher than the SUSY breaking scale. Unlike the standard GMSB soft terms, these new terms break the global symmetry of the PQ NMSSM, $U(1)_{\text{PQ}}$, whose existence is at the origin of the $\kappa = 0$ choice. In the string theory setup, $U(1)_{\text{PQ}}$ is a remnant of a local gauge symmetry which has been spontaneously broken. As is well known, the corresponding gauge boson acquires a large (GUT scale) mass through the Green-Schwarz mechanism [29]. Here we break $U(1)_{\text{PQ}}$ through the vev of a scalar field X , which will also play the additional role of the SUSY breaking spurion.

On the other hand, we show that despite the presence of these extra large-scale terms the model does *not* present fine-tuning levels higher than those already present in its MSSM version, i.e., $\sim 10^4$. This is due to a cancellation among some specific terms entering the fine-tuning measure, because of relations determined by our UV completion. Thus, this model is partially immune from the mild “tadpole problem” [30–37] of the General NMSSM [38], according to which the extra terms dramatically amplify the effective theory’s sensitivity to the high energy physics.

The paper is organized as follows. In section 2 we introduce the model. We start from the flavored GMSB structure of the superpotential and progress subsequently to introducing one by one the additional terms that will define our version of the PQ NMSSM. In section 3 we perform a numerical analysis of the model. We identify the regions of the parameter space consistent with the constraints from the Higgs mass measurement and LHC searches, and we provide some benchmark points useful for the discussion and also possible collider signatures. In section 4 we discuss the fine tuning of the model, and prove that it is not larger than the present level found in the MSSM, despite the presence of tadpole and quadratic terms in the singlet field. We finally provide our summary and concluding remarks in section 5.

Additionally, we provide four appendices to the text, dedicated, respectively, to the GMSB calculation of the soft masses in the model; to the explicit calculation of the $U(1)_{PQ}$ breaking effective terms of the superpotential and soft Lagrangian; to the explicit estimate of the size of our constants; and to the explicit form of the tree-level Higgs mass in the PQ NMSSM.

2 The model

2.1 Flavored GMSB with hierarchical Yukawa couplings

A simple model combining the advantages of F-theory model building and flavored GMSB was introduced in [20]. Since the visible matter and the messengers have the same origin they should also present a common hierarchical structure of their couplings, e.g., a structure of the Froggatt-Nielsen type [1]. This reasoning basically implies that the messengers are in **5** representations of $SU(5)$. The simplest construction of this type contains three chiral families of **10**s, four $\bar{\mathbf{5}}$ s and one extra multiplet $\mathbf{5}_Y$, which is necessary to form a vector pair of messengers and cancel the resulting anomalies.

The relevant superpotential terms using $SU(5)$ representations at the GUT scale are

$$W \supset \sum_{i,j} y_{ij}^u \mathbf{10}_i \mathbf{10}_j (\mathbf{5}_H)_2 + \sum_{i,J} \hat{y}_{iJ} \mathbf{10}_i \bar{\mathbf{5}}_J (\bar{\mathbf{5}}_H)_2 + \left(\sum_J a_J \bar{\mathbf{5}}_J \right) \mathbf{5}_Y X, \quad (2.1)$$

where in eq. (2.1) flavor indices run as $i, j = 1, 2, 3$ and $J = 1, 2, 3, 4$, and the subscript “2” attached to the Higgs fields highlights that we take into account only the doublet part of the $\mathbf{5}_H$ and $\bar{\mathbf{5}}_H$ Higgs multiplets. In this regard, we recall here that in F-theory GUTs doublet-triplet splitting can be obtained through an appropriate choice of internal fluxes (see, e.g., sections 10.3 and 12 of ref. [5]).

We assume that all the couplings in eq. (2.1) have a hierarchical structure, i.e., $y_{ij}^u \ll y_{i+1,j}^u$, $y_{ij}^u \ll y_{i,j+1}^u$ for all i, j (and similarly for the \hat{y}_{iJ}), and also $a_J \ll a_{J+1}$. One can claim [7] that the couplings with top-most indices, y_{33}^u , \hat{y}_{34} , and a_4 are all of the same order. The measured value of the top quark mass sets $y_t = y_{33}^u$ to be of $\mathcal{O}(1)$ if the renormalization group (RG) flow does not change y_t drastically. Note also that, as was mentioned in section 1, the hierarchy of the couplings is better enforced for values of $\tan \beta$ not much larger than 1, as $\hat{y}_{33}/\hat{y}_{34} \sim \tan \beta m_b/m_t$.

The spurion X acquires a vacuum expectation value (vev), $\langle X \rangle$, which gives a mass, $M_Y = \langle X \rangle$, to the messengers $\mathbf{5}_Y$ and $\bar{\mathbf{5}}_Y$, where $\bar{\mathbf{5}}_Y = \sum_J a_J \bar{\mathbf{5}}_J$. The other $\bar{\mathbf{5}}_s$ remain massless. The spurion also triggers SUSY breaking through its nontrivial F -term: $\hat{X} \rightarrow \langle X \rangle + \theta^2 F_X$. We assume here that the dynamics of the spurion is governed by the physics of the high scale, so that it is effectively a non-dynamical field below the messenger scale.

After diagonalizing the mass matrices in eq. (2.1), we can write down the terms with $\mathcal{O}(1)$ couplings that will be relevant for our analysis:

$$W \supset y_t \mathbf{10}_3 \mathbf{10}_3 (\mathbf{5}_H)_2 + h_3 \mathbf{10}_3 \bar{\mathbf{5}}_Y (\bar{\mathbf{5}}_H)_2 + \bar{\mathbf{5}}_Y \mathbf{5}_Y X, \quad (2.2)$$

where $y_t \approx 1$, $h_3 \equiv \hat{y}_{34} \approx 1$. By integrating out the messengers one can obtain the soft terms of the MSSM explicitly displayed in appendix A.

2.2 NMSSM GMSB with PQ symmetry

In the NMSSM one introduces an extra chiral superfield S , whose vev generates the μ term at the electroweak (EW) scale. We consider here the hypothesis that the fields of the model are charged under a PQ symmetry, $U(1)_{\text{PQ}}$, which introduces additional restrictions on the possible couplings. In particular, as we shall see below, it forbids any superpotential term for S alone ($\kappa = 0$). We also assume that the PQ charges of the X and S fields are opposite in sign, $q(S) = -q(X)$ (as considered, e.g., in [6]), which leads to certain necessary terms in the Lagrangian. Incidentally, $U(1)_{\text{PQ}}$ also helps prevent fast baryon decay due to GUT processes [39].

The resulting $U(1)_{\text{PQ}}$ charges are summarized in the following table:

	$\mathbf{10}_{1,2,3}$	$\bar{\mathbf{5}}_{1,2,3}, \bar{\mathbf{5}}_Y$	$\mathbf{5}_H$	$\bar{\mathbf{5}}_H$	$\mathbf{5}_Y$	S	X
q	+1/4	+1/4	-1/2	-1/2	+3/4	+1	-1

(2.3)

where the charges are normalized in such a way that the largest one equals 1. Note that this implies that the spurion X does not couple to the Higgs fields, while S cannot couple to the messengers in dimension 4 operators. Moreover, as mentioned above, there cannot exist polynomial couplings in S and X alone so that, e.g., $\kappa = 0$ in the notation of the usual \mathbb{Z}^3 -symmetric NMSSM [40].

In summary, the only renormalizable superpotential term preserving $U(1)_{\text{PQ}}$ and containing S is¹

$$W_S = \lambda S H_u H_d, \quad (2.4)$$

¹We drop here the mass term XS , which is unnatural in F-theoretic constructions, see appendix B.

which after SUSY breaking gives rise to a trilinear soft Lagrangian contribution, A_λ , and a scalar soft mass for the singlet, m_S^2 ,

$$-L_{S,\text{soft}} = \lambda A_\lambda H_u H_d S + m_S^2 |S|^2, \quad (2.5)$$

whose explicit expression in terms of the GMSB parameters is given in appendix A.

As one can easily see, $U(1)_{\text{PQ}}$ is anomalous. It is known that the anomaly can be canceled by the Green-Schwartz mechanism [29], which gives a mass to the $U(1)_{\text{PQ}}$ gauge boson of the order of M_{GUT} .

Note that $\langle X \rangle$ breaks $U(1)_{\text{PQ}}$, so that at low energies there appear additional effective $U(1)_{\text{PQ}}$ breaking interaction terms. We present them in the next subsection and discuss them in detail in appendix B.

2.3 Effective interactions below the messenger scale

In addition to (2.4) and (2.5), other contributions to the superpotential and soft Lagrangian might arise below M_Y . As we explain in appendix B, these can be due, for example, to instanton effects, exchange of heavy chiral $U(1)_{\text{PQ}}$ neutral superfields, exchange of heavy gauge bosons, or Giudice-Masiero [41] effective terms in the Kähler potential. The most important terms for the low-energy dynamics will be those containing powers of the spurion superfield, X , because X receives a large vev.

Additional terms to the superpotential and soft SUSY-breaking Lagrangian take the form

$$\delta W_S = \xi_F S + \frac{1}{2} \mu' S^2, \quad (2.6)$$

$$-\delta L_{S,\text{soft}} = \delta m_S^2 |S|^2 + \left(\frac{1}{2} m_S'^2 S^2 + \xi_S S + \text{h.c.} \right), \quad (2.7)$$

where we have used the standard notation of [40] and we do not explicitly distinguish between the superfields and their scalar components. Importantly, to a very good approximation the relations

$$\kappa \approx 0 \text{ and } A_\kappa \approx 0 \quad (2.8)$$

still hold, even while there are other massive couplings that effectively break $U(1)_{\text{PQ}}$.

The superpotential and Lagrangian elements in eqs. (2.6) and (2.7) are best expressed in terms of $x = M_Y/M_{\text{GUT}}$ and $\Lambda = F_X/M_Y$. They are given by (see appendix B for full details)

$$\begin{aligned} \delta m_S^2 &= -|\lambda_\Psi|^2 |\Lambda|^2 x^2, \\ \xi_F &= I_{1,3} M_{\text{GUT}}^2 x^2, \\ \mu' &= -\lambda_\Psi^2 M_{\text{GUT}} x^2, \\ \xi_S &= -2I_{1,3} \Lambda M_{\text{GUT}}^2 x^2 = -2\xi_F \Lambda, \\ m_S'^2 &= 2\lambda_\Psi^2 \Lambda M_{\text{GUT}} x^2 = -2\mu' \Lambda, \end{aligned} \quad (2.9)$$

where $I_{1,3}$ is a dimensionless instanton contribution, and λ_Ψ is a $\mathcal{O}(1)$ “Yukawa” coupling between the X and S superfields and a heavy chiral $U(1)_{\text{PQ}}$ neutral superfield, Ψ , that is

integrated out below M_{GUT} . Without loss of generality, in what follows we fix $M_{\text{GUT}} = 2 \times 10^{16} \text{ GeV}$ and $\lambda_\Psi = 1$.

All the soft terms and superpotential parameters in eqs. (2.9) are defined at M_Y and then renormalized to lower energy through RG flow. The model is therefore described entirely by 5 free parameters defined at the messenger scale:

$$M_Y \text{ (or } x), \Lambda, h_3, \lambda, \xi_F, \quad (2.10)$$

where we have used the more familiar superpotential tadpole ξ_F in place of the numerical instanton coefficient $I_{1,3}$. As will be clear below, from a phenomenological point of view one is interested in a somewhat limited range of Λ , so that the number of really free parameters can then be reduced to 4, of which only 2, x and ξ_F , set the overall scale of the additional terms in eqs. (2.6)–(2.7).

We want to highlight here that

$$\frac{\xi_S}{\xi_F} = \frac{m_S'^2}{\mu'}, \quad (2.11)$$

which holds up to leading terms (see appendix C). Equation (2.11) is RG invariant after suppressing subdominant terms in the RG equations. This characteristic will turn out to be essential to reducing the fine tuning of the model by approximately two orders of magnitude, thus largely ameliorating the tadpole problem, as we discuss in detail in section 4.

3 Phenomenological analysis

In this sections we present the results of our numerical analysis, which determines the phenomenological constraints on the parameter space of the model and possible signatures at present and future experiments. In practice, the most important constraints come from the measurement of the Higgs boson mass, $m_{h_1} \approx 125 \text{ GeV}$ [42, 43] and the bounds from direct searches for SUSY at the LHC, of which the most relevant are the ones on the gluino mass, $m_{\tilde{g}} \gtrsim 1.5 \times 10^3 \text{ GeV}$ [44–46], and on heavy stable charged particles [47].

We calculate spectra and NMSSM parameters with `NMSSMTools v4.5.1` [48], which we modified to incorporate the h_3 -dependent and λ -dependent contributions to the soft terms given in eqs. (A.1) of appendix A, and the additional masses and tadpoles defined in eqs. (2.9).

To guide the scanning procedure we use `MultiNest` [49]. We scan with flat priors in the parameters Λ , M_Y , $\lambda(M_{\text{SUSY}})$, h_3 , and $\tan \beta$. The fundamental parameter $\lambda(M_Y)$ has been traded for the renormalized value of λ at the scale of the geometrical average of the stop masses, M_{SUSY} ; the fundamental parameter ξ_F has been traded for the ratio of the Higgs doublets' vevs, $\tan \beta$, through the electroweak symmetry breaking (EWSB) conditions.

We scan in the following ranges:

$$\begin{aligned} 10^5 \text{ GeV} \leq \Lambda \leq 10^6 \text{ GeV}, \quad 10^9 \text{ GeV} \leq M_Y \leq 10^{14} \text{ GeV}, \\ 0.1 \leq h_3 \leq 1, \quad 0.1 \leq \lambda(M_{\text{SUSY}}) \leq 2, \quad 1 \leq \tan \beta \leq 8. \end{aligned} \quad (3.1)$$

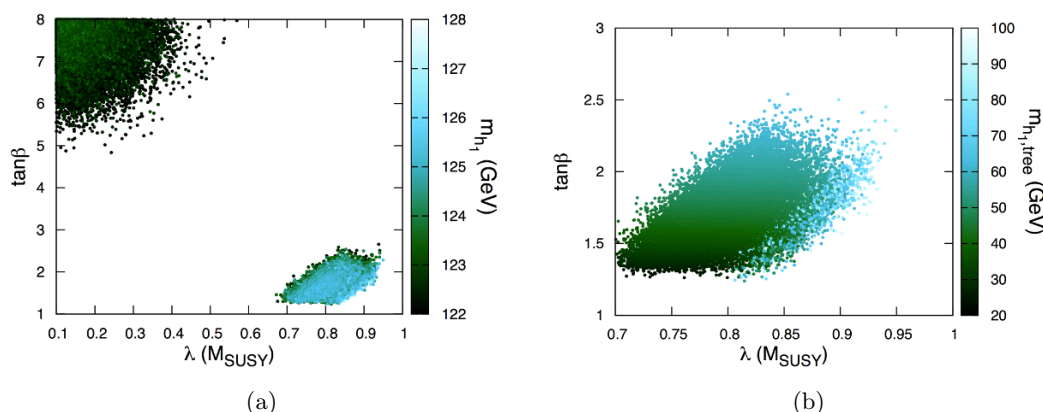


Figure 1. (a) The lightest Higgs mass value for the points within the 1σ theoretical uncertainty, $122 \text{ GeV} \lesssim m_{h_1} \lesssim 128 \text{ GeV}$, in the $(\lambda(M_{\text{SUSY}}), \tan\beta)$ plane. (b) A zoom of the region of large λ , where we plot the tree-level value of the Higgs mass in the $(\lambda(M_{\text{SUSY}}), \tan\beta)$ plane.

As was mentioned above, the LHC lower bound on the gluino mass affects the choice of scanning range for Λ , which we constrain to a narrow interval, as the soft masses of the gluino and the bino strongly depend on this parameter. Below $\Lambda \approx 10^5 \text{ GeV}$ the gluino tends to become too light, while for $\Lambda > 10^6 \text{ GeV}$ the model becomes substantially and uncomfortably more fine-tuned. The lower bound on M_Y comes from requiring the two-loop GMSB expression of eqs. (A.1) to be the dominant contribution to the soft masses, while the upper bound comes from the requirement of being well within the range of validity of the effective theory below M_{GUT} : for $M_Y > 10^{14} \text{ GeV}$, the first-order expansion at the origin of eqs. (2.9) is not well-justified. Note finally, that we allow for a wide range of λ values, to counterbalance our choice of low $\tan\beta$.

In addition to the fundamental parameters we scan in some of the SM nuisance parameters: the strong coupling constant, the \overline{MS} value of the bottom quark mass, and the top quark pole mass, which we include in the likelihood function. For these we adopt normal distributions based on the most recent PDG [50] central values and experimental uncertainties. The scans are driven by a Gaussian likelihood function for the experimental measurement of the Higgs mass, where we added to the experimental uncertainties, in quadrature, a theoretical uncertainty of approximately 3 GeV . This choice is motivated by the large uncertainty still present in the calculation of the Higgs mass, which includes the choice of renormalization scheme, missing higher order contributions, and numerical differences between various existing public codes (see [51] for a recent discussion).

In figure 1(a) we show the value of the lightest Higgs mass for the points within the 1σ theoretical uncertainty, $122 \text{ GeV} \lesssim m_{h_1} \lesssim 128 \text{ GeV}$, in the $(\lambda(M_{\text{SUSY}}), \tan\beta)$ plane. One can easily recognize two different regions. The first is characterized by $\lambda \approx 0.1 - 0.5$ and $\tan\beta \gtrsim 5$, and the scan seems to give there a Higgs mass slightly low, $m_{h_1} \lesssim 124 \text{ GeV}$, albeit well within the adopted theoretical uncertainty. This “small- λ ” region shows solutions similar to the MSSM limit of the model [21]. The Higgs mass decreases for lower values of $\tan\beta$, as a consequence of the rapid drop in the tree-level value, but it also decreases

slowly for $\lambda > 0.4 - 0.5$ when $\tan\beta \gtrsim 7$. For the majority of the points this is due to the trilinear term $|A_t|$ becoming smaller as λ increases,² as the scan cannot compensate this effect by raising M_{SUSY} because of our narrow range in Λ .

A second region, more interesting for the purposes of this paper, can be found instead at $\lambda \gtrsim 0.7$ and $\tan\beta \lesssim 3$. As figure 1(a) shows, the Higgs mass there can comfortably reach the measured value and above. However, not all the points in this region are equivalent to each other, as an analysis of the tree-level Higgs mass can show.

In figure 1(b) we present a zoomed-in detail of the “large- λ ” region, where we plot in the third dimension the tree-level value of the Higgs mass, whose explicit expression is presented in appendix D. Figure 1(b) shows two distinct sets of points, characterized by different properties. For $\lambda > 0.8$ there are points characterized by tree-level masses in the range $\sim 70 - 90$ GeV. These solutions are somewhat similar to models of λSUSY [52], characterized by values of λ that can become non perturbative before reaching the GUT scale.³ The tree-level mass is enhanced with respect to the MSSM value, and as a consequence the needed radiative corrections are less substantial than in the MSSM for equivalent $\tan\beta$. Note, however, that we could not find a single region of the parameter space in which $m_{h_1, \text{tree}}^2 > M_Z^2$, so that significant radiative corrections are *always* necessary in this model to obtain the correct Higgs mass.

Still, these points present somewhat lighter spectra than in the rest of the parameter space, although for the most part still too heavy to be significantly probed in Run II at the LHC [53]. The lightest gluino mass found by the scan is around 2 TeV, as can be seen in table 1, where we present the parameters and spectral properties of a typical point (BP1).

Several points in figure 1(b) are characterized by a relatively low value of the tree-level Higgs mass, $m_{h_1, \text{tree}}^2 \approx 20 - 60$ GeV, despite sizeable values of λ . This can be understood from eq. (D.3) in appendix D, which shows that for low $\tan\beta$ the MSSM-like part of the tree-level Higgs mass is augmented in the PQ NMSSM by an extra term which is approximately $\delta m_{h_1, \text{tree}}^2 \approx \lambda^2 v^2 \epsilon$, where $\epsilon = \xi_S / (\xi_F \mu')$ assumes in our model values in the range $\sim 0 - 0.8$. Thus, the tadpole ratio significantly affects the value of the tree-level mass: if $\xi_S \ll \xi_F \mu'$ the tree-level mass is approximately equal to its typical MSSM value, as is exactly the case for these points.

For $\lambda \gtrsim 0.7$, these solutions can still quite comfortably reach $m_{h_1} \approx 125$ GeV thanks to very large λ -dependent radiative corrections. A representative point of this region (BP2) can be found in table 1. One can see that BP2 is characterized by a large messenger scale, $M_Y \approx 10^{14}$ GeV, which is necessary to lift the heavy Higgs masses up and boost the Higgs-loops corrections to the lightest Higgs mass. As can be expected, these points are marred by extremely high levels of fine tuning, because of the large sensitivity to λ -driven radiative corrections. Thus, we will not discuss them further in what follows.

²Recall the RGEs for A_t : $dA_t/dt \sim \lambda^2 A_\lambda$ [40], where $A_\lambda < 0$, see, e.g., the second to last of (A.1) in appendix A.

³Since there are no direct couplings between the scalar S and the messengers, and S is also a gauge singlet, at one loop no additional terms arise in the β_λ above M_Y . The gauge couplings g_1 and g_2 enter β_λ and in the presence of the messengers can get renormalized slightly more strongly. We have checked numerically that the effect is however very small and does not change the fact that $\lambda > 0.8$ generally becomes nonperturbative at the GUT scale.

Benchmark	BP1	BP2	BP3	BP4
Model parameters (at M_Y)				
Λ	$2.98 \times 10^5 \text{ GeV}$	$5.79 \times 10^5 \text{ GeV}$	$5.92 \times 10^5 \text{ GeV}$	$9.15 \times 10^5 \text{ GeV}$
M_Y	$2.49 \times 10^{11} \text{ GeV}$	$5.99 \times 10^{13} \text{ GeV}$	$9.56 \times 10^{11} \text{ GeV}$	$2.48 \times 10^{13} \text{ GeV}$
h_3	0.92	0.65	0.73	0.23
λ	1.72	1.69	0.14	0.35
ξ_F	$2.14 \times 10^{10} \text{ GeV}^2$	$2.03 \times 10^{15} \text{ GeV}^2$	$1.23 \times 10^{12} \text{ GeV}^2$	$3.70 \times 10^{14} \text{ GeV}^2$
Relevant for EWSB (at M_{SUSY})				
$\tan \beta$	1.70	1.40	7.52	7.46
$m_{H_d}^2$	$4.33 \times 10^7 \text{ GeV}^2$	$4.39 \times 10^7 \text{ GeV}^2$	$8.95 \times 10^6 \text{ GeV}^2$	$-8.13 \times 10^6 \text{ GeV}^2$
$m_{H_u}^2$	$-2.24 \times 10^7 \text{ GeV}^2$	$-3.19 \times 10^7 \text{ GeV}^2$	$-1.21 \times 10^7 \text{ GeV}^2$	$-1.51 \times 10^7 \text{ GeV}^2$
λ	0.82	0.70	0.13	0.33
μ_{eff}	7639 GeV	10746 GeV	3596 GeV	4048 GeV
A_λ	-1746 GeV	-1353 GeV	-7635 GeV	-1075 GeV
m_S^2	$-4.90 \times 10^7 \text{ GeV}^2$	$-6.94 \times 10^7 \text{ GeV}^2$	$-1.71 \times 10^6 \text{ GeV}^2$	$-2.28 \times 10^6 \text{ GeV}^2$
μ'	$-1.69 \times 10^6 \text{ GeV}$	$-9.66 \times 10^{10} \text{ GeV}$	$-4.53 \times 10^7 \text{ GeV}$	$-2.89 \times 10^{10} \text{ GeV}$
$m_S'^2$	$1.00 \times 10^{12} \text{ GeV}^2$	$1.11 \times 10^{17} \text{ GeV}^2$	$5.37 \times 10^{13} \text{ GeV}^2$	$5.28 \times 10^{16} \text{ GeV}^2$
ξ_F	$1.58 \times 10^{10} \text{ GeV}^2$	$1.49 \times 10^{15} \text{ GeV}^2$	$1.23 \times 10^{12} \text{ GeV}^2$	$3.58 \times 10^{14} \text{ GeV}^2$
ξ_S	$-9.17 \times 10^{15} \text{ GeV}^3$	$-1.70 \times 10^{21} \text{ GeV}^3$	$-1.44 \times 10^{18} \text{ GeV}^3$	$-6.55 \times 10^{20} \text{ GeV}^3$
Max fine tuning	$\sim 10^4 (\lambda, \xi_F)$	$\sim 10^6 (\lambda)$	$\sim 10^4 (\xi_F)$	$\sim 10^4 (\xi_F)$
Spectrum				
$m_{h_1, \text{tree}}$	74.1 GeV	27.7 GeV	84.6 GeV	84.1 GeV
m_{h_1}	123.5 GeV	123.0 GeV	122.6 GeV	122.3 GeV
m_{h_2}, m_{a_1}	$5.86 \times 10^4 \text{ GeV}$	$2.23 \times 10^7 \text{ GeV}$	$7.11 \times 10^4 \text{ GeV}$	$5.91 \times 10^6 \text{ GeV}$
$m_{\tilde{g}}$	2170 GeV	3959 GeV	4006 GeV	5970 GeV
$m_{\tilde{t}_1}$	2311 GeV	3759 GeV	3436 GeV	5509 GeV
$m_{\chi_1^0}$	422 GeV	813 GeV	819 GeV	1266 GeV
$m_{\chi_1^\pm}$	832 GeV	1563 GeV	1550 GeV	2355 GeV
$m_{\tilde{\tau}_1}$	920 GeV	2170 GeV	2391 GeV	261 GeV

Table 1. The model fundamental parameters at M_Y , the corresponding parameter values at M_{SUSY} , fine tuning, and spectra of four benchmark points discussed in section 3. The parameters in parentheses give the maximal contribution to the fine-tuning measure.

The third benchmark point in table 1 (BP3) is representative of the small- λ , almost MSSM-like region shown in figure 1(a) and discussed above. With respect to the large- λ region (see BP1), the lightest points in the small- λ region tend to present gluino and neutralino masses approximately a factor 2 heavier than the lightest points with large λ . Note that the fine tuning of the small- and large- λ regions are very comparable.

A discussion of the fine tuning of the model is presented in section 4. The model is tuned at least to the level of 5×10^3 – 10^4 , but it is interesting to note that, particularly for the points of the small- λ region, which present equivalent MSSM solutions in the limit $\lambda \rightarrow 0$, the fine tuning is not higher than it would be in the MSSM, even if in the PQ NMSSM presented here we had to introduce additional large scale terms that enter the EWSB conditions: ξ_F , ξ_S , μ' , and $m_S'^2$. In fact, we will show in section 4 that UV relations between these parameters allow for significant cancellations in the fine-tuning measure, so that this does not increase proportionally to the typical scale of the extra terms.

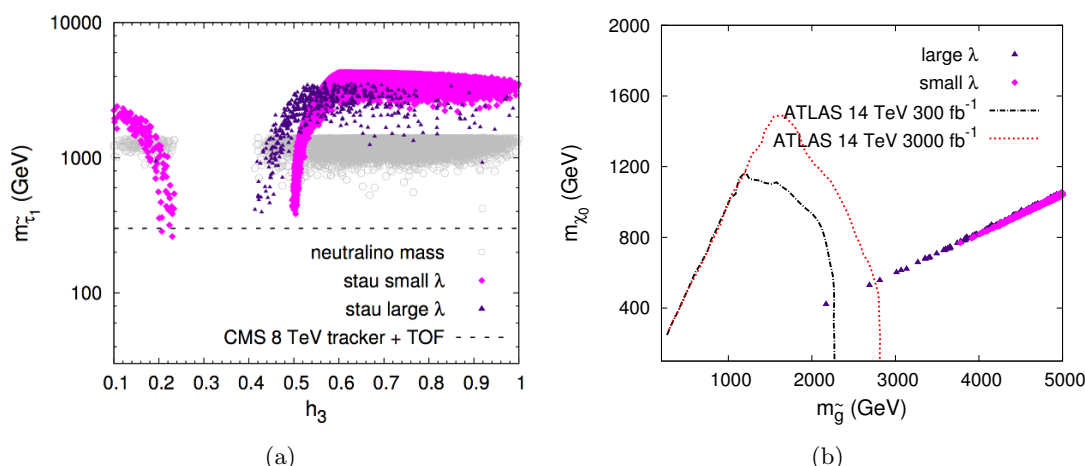


Figure 2. (a) The distributions of the lightest stau mass, $m_{\tilde{\tau}_1}$ as a function of h_3 for the points of the small- λ region (magenta diamonds) and of the large- λ region (indigo triangles). The neutralino mass is plotted in the background, as gray circles. The dashed black line shows the 95% C.L. lower mass bound on heavy stable charged particles from the tracker + TOF analysis at CMS 8 TeV [47]. (b) The ATLAS projections for gluino searches at the LHC 14 TeV [53] compared to the viable points of our model. The dot-dashed black line shown the 95% C.L. expected exclusion reach with 300 fb^{-1} and the dotted red line the reach with 3000 fb^{-1} .

The parameter h_3 , which is responsible for the mixing between the messenger and matter sector, cannot span the entire range of eq. (3.1): there is a gap in its allowed values, which was already observed for the MSSM in [21]. The reason can be easily understood by a quick analysis of eqs. (A.1) in appendix A. The staus can become tachyonic when a cancellation takes place between terms dominated by the gauge couplings and those dominated by h_3 . The position and range of this gap strongly depend on the values of λ , and the gap tends to become smaller for larger λ values.

In figure 2(a) we show the distribution of the stau mass as a function of h_3 for the small- λ (magenta diamonds) and large- λ (indigo triangles) regions. The stau mass can drop drastically as one approaches the critical values of h_3 giving rise to this cancellation, to the point that it becomes the Next-to-lightest SUSY particle (the LSP is the gravitino), as a comparison with the neutralino mass, plotted here with gray circles, shows.

This brings about the interesting possibility of testing selected h_3 regions by searches for heavy stable charged particles. We plot in figure 2(a) with a black dashed line the 95% C.L. lower bound on the mass of the stable stau from an analysis of long time-of-flight (TOF) to the outer muon system and anomalously high (or low) energy deposition in the inner tracker at CMS, with 8 TeV data [47]. The search excludes cross sections of the order of 1.5 fb or above for pair production of ~ 300 GeV stable staus, which is in agreement with what one obtains in this model with typical spectra and a stau NLSP with a mass of 300 GeV. We thus expect that the corresponding search in Run II will start biting into specific regions of our parameter space: $h_3 \approx 0.2$ or 0.5 for $\lambda < 0.4$; $h_3 \approx 0.4$ for $\lambda \approx 0.85 - 0.9$. We show a representative point with stau NLSP (BP4) in table 1.

We conclude this section by comparing in figure 2(b) the projected [53] exclusion reach for gluino masses at ATLAS 14 TeV with our model's predictions. Again, points of the large- λ region are shown as indigo triangles and points of small λ as magenta diamonds. The 95% C.L. expected reach with 300 fb^{-1} of integrated luminosity in searches with jets + missing E_T is shown as a dot-dashed black line. As is well known, in GMSB models specific LHC phenomenology is strongly affected by the effective coupling of the neutralino (which is predominantly bino-like in our model) and the gravitino. However, gluino searches at 8 TeV have shown that the mass bounds do not significantly depend on whether the neutralino is long-lived enough to escape the detector [44, 46], or it decays promptly producing photons [45]. Thus, for the purpose of this paper we accept the projected reach of [53] as a reasonable estimate.

One can see in figure 2(b), that the points of the large- λ region might begin to be probed at the very end of the LHC Run II, particularly if the High-Luminosity LHC [54], whose reach [53] is shown as a dotted red line, is approved. However, figure 2(b) more realistically shows that the structure devised here yields spectra too heavy to be significantly tested at the LHC, and a high-energy collider will be necessary. It might be interesting to study the reach of a 100 TeV collider for this model, and we leave this for future work.

4 Fine tuning

We dedicate this section to the calculation of the fine tuning of the model. As was mentioned in section 3, it turns out that this is smaller than what one could expect from naive estimates based on a rough order-of-magnitude analysis. We take the maximum of the fine tuning due to each of the fundamental parameters of eq. (2.10), which we calculate according to the Barbieri-Giudice measure [55, 56].

By indicating the parameters of eq. (2.10) collectively as p_i , one must calculate the max of the

$$\Delta_{p_i} = \frac{\partial \log M_Z^2}{\partial \log p_i} = \frac{p_i}{M_Z^2} \frac{\partial M_Z^2}{\partial p_i} \quad (\text{order of magnitude only}). \quad (4.1)$$

Given the three EWSB conditions that determine the values of the Higgs vevs,⁴

$$\text{EWSB}_j(M_Z^2, \tan \beta, s, \mu', \xi_S, m_S'^2 \dots; p_i) = 0 \quad \text{for } j = 1, 2, 3, \quad (4.2)$$

one can apply the chain rule,

$$\frac{\partial P_k}{\partial p_i} = \left[\frac{\partial(\text{EWSB}_j)}{\partial P_k} \right]^{-1} \frac{\partial(\text{EWSB}_j)}{\partial p_i}, \quad (4.3)$$

where the 3×3 matrix in the jk indices is built out of the partial derivatives with respect to $P_k = \{M_Z^2, \tan \beta, s\}$, and one is interested in the numerical value of the first row in the system (4.3), $\partial M_Z^2 / \partial p_i$.

⁴The explicit forms of EWSB_1 , EWSB_2 , and EWSB_3 can be found in eqs. (C.1)–(C.3) of appendix C.

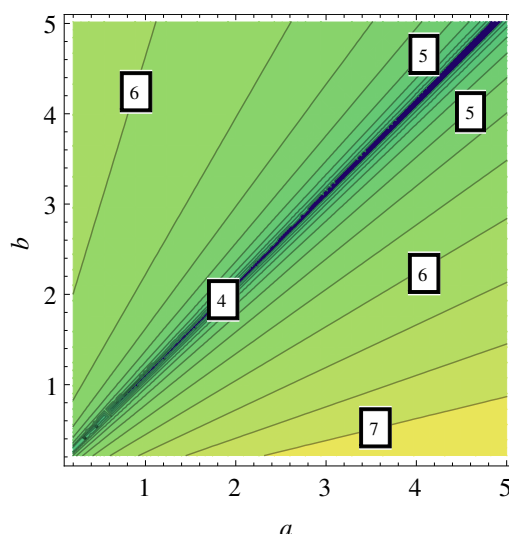


Figure 3. A plot of $\log_{10} \Delta_{\xi_F}$ for BP1 of table 1 as a function of the arbitrary real coefficient a, b .

Despite the presence of large contributions to EWSB from the tadpoles and other terms, a numerical calculation shows that the partial derivatives are sensitive to cancellations. To see this, we parametrize two large parameters, ξ_S and $m_S'^2$, in the following way:

$$\xi_S = -a\Lambda\xi_F, \quad m_S'^2 = -b\Lambda\mu', \quad (4.4)$$

where a and b are arbitrary real numbers, and we proceed to the calculation of Δ_{ξ_F} and Δ_{M_Y} for changing a and b . M_Y , which directly enters the definition of μ' , and ξ_F are the largest remaining free parameters in the theory.

We show in figure 3 a plot of $\log_{10} \Delta_{\xi_F}$ in the (a, b) plane for BP1. A plot of $\log_{10} \Delta_{M_Y}$ shows similar behavior and we do not present it here. One can clearly see that the fine tuning is reduced by more than two orders of magnitude when $a \approx b$.

One can see from eqs. (B.8) and (B.9) of appendix B that in our model $b = 2$ is a consequence of breaking SUSY via the spurion. As a consequence, according to figure 3, one needs $a \approx 2$ to lower the fine tuning to $\sim 10^4$. As is explained in appendix B after eq. (B.4), we make here a reasonable assumption, that there exist selection rules in the stringy UV completion that allow one to generate only the instanton contributions that lead to $a = 2$. Note that, as one can see in eqs. (B.13) and following paragraph, the terms depending on λ_μ are much smaller than the instanton contribution to ξ_S , so that $\lambda_\mu \neq 0$ will not cause significant deviations from $a = 2$.

The cancellations described here have their origin in the specific form of the tree-level EWSB conditions. They lead to the fine-tuning levels of the benchmark points in table 1, and in general similar values are obtained over the whole viable parameter space. Thus, as was anticipated in section 1, our model is partially protected from the tadpole problem, provided an appropriate relation of the kind of (4.4) is given by the UV completion.

5 Summary and conclusions

In this paper, motivated by the desire of maintaining a Yukawa flavor structure in agreement with UV completions based on F-theory, we have used flavored gauge mediation to construct a specific version of the Peccei-Quinn NMSSM. Considerations concerning the stringy UV completion lead to a very predictive version of the model, which depends on a few free parameters.

We have performed a thorough numerical study of the parameter space of the model and confronted it with the phenomenological constraints. Our findings are supported by analytical arguments. We showed that the PQ NMSSM exhibits unusual properties, specifically it requires relatively large nonstandard terms: tadpole coefficients ξ_F , ξ_S , and quadratic terms depending on μ' and m_S^2 . In spite of this, we showed that the fine tuning is not greater than in the MSSM thanks to a special relation between the ratios ξ_S/ξ_F and m_S^2/μ' , which originates in the specific UV completion considered here, and which results in a cancellation in the fine-tuning measure. Thus, we showed that this version of the the PQ NMSSM is partially immune from the mild tadpole problem typical of many general versions of the NMSSM.

We found that the model can easily accommodate the Higgs mass at 125 GeV, but the spectra can possibly be in reach of the LHC only in a region of the parameter space characterized by $\lambda > 0.8$ which, as is well known, implies that the renormalized value of λ at the GUT scale might incur a Landau pole. In general, we were not able to find a single parameter space region over which the tree-level value of the lightest Higgs mass is larger than the Z boson mass, although it can be enhanced with respect to its MSSM counterpart in regions of large λ and small $\tan\beta$. In all cases, however, $m_{h_1} \approx 125$ GeV requires substantial radiative correction and a certain level of fine tuning, of the order of 10^4 , cannot be avoided.

In spite of these interesting formal properties, we found that the phenomenology of the model is quite standard, with typical spectra being too heavy to be significantly probed at the LHC. However, small regions of the parameter space exist featuring gluino masses around 2 TeV, for a bino-like neutralino mass of ~ 400 GeV. These might begin to be probed at the end of Run II in gluino searches. For particular choices of the parameter h_3 , which in our model determines the mixing between the messengers and matter sector, the NLSP is a stau with a mass $\gtrsim 300$ GeV, and a cross section right in the ballpark of the range currently probed by searches for heavy stable charged particles at CMS, which will be able to further constrain part of the parameter space with 13 and 14 TeV data.

This work can be extended in several directions. An open question remains concerning the dynamics of the spurion X , which should result from a UV completion of the model (supergravity or a string compactification with fluxes). It is of course possible that most of the necessary ingredients are contained in appendix B, with the exception of some self-interaction terms in X . In that case, including spurion quanta into the analysis should not pose a difficult task.

Another possibility would be to enlarge the size of the corrections given by exchange of the $U(1)_{PQ}$ gauge bosons by increasing the strength of the g_{PQ} coupling. This would

amend the soft terms given in appendix A by possibly substantial corrections. Finally, one could lower the messenger mass, which would result in a modification of the soft masses by one-loop terms.

The list of modifications is of course much longer, and we leave this extended discussion to a future publication.

Acknowledgments

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A Soft terms

At the leading order, all soft masses and trilinear couplings are generated at the messenger scale $M_Y = \langle X \rangle$. While deriving the explicit formulas, we will make some simplifying assumptions.

First of all recall that eq. (2.2) is defined at M_{GUT} . Evolution to M_Y leads to further mixing between matter and messengers. However, we have explicitly checked that this has a very mild influence on the structure and values of the SM Yukawa couplings and h_3 at M_Y . Secondly, we take into account only the leading superpotential contributions, eq. (2.2), thus disregarding all other contributions from eq. (2.1), which are usually much smaller. In particular, we neglect the terms proportional to the bottom and tau Yukawa couplings.

In the end, all the soft terms depend only on $\Lambda = F_X/\langle X \rangle$, λ , $h_3 = \hat{y}_{34}$, $y_t = y_{33}^u$, and the gauge coupling constants, while the dependence on the scale M_Y appears through the RG evolution.

We adopt here the general formulas derived in [11, 57] in the presence of MSSM-messenger superpotential interactions, which provide a good approximation for the case at hand. The resulting soft terms are thus

$$\begin{aligned}
 (m_{\tilde{Q}})_{ij}^2 &= \frac{\Lambda^2}{3840\pi^4} \left\{ \delta_{ij} 8\pi^2 (\alpha_1^2 + 45\alpha_2^2 + 80\alpha_3^2) \right. \\
 &\quad \left. + \delta_{i3}\delta_{j3} |h_3|^2 [105|h_3|^2 - 4\pi(7\alpha_1 + 45\alpha_2 + 80\alpha_3)] \right\}, \\
 (m_{\tilde{U}})_{ij}^2 &= \frac{\Lambda^2}{30\pi^4} \left[\delta_{ij} \pi^2 (\alpha_1^2 + 5\alpha_3^2) - \delta_{i3}\delta_{j3} \frac{15}{64} |y_t|^2 |h_3|^2 \right], \\
 (m_{\tilde{D}})_{ij}^2 &= \frac{\Lambda^2}{120\pi^4} [\delta_{ij} \pi^2 (\alpha_1^2 + 20\alpha_3^2)], \\
 (m_{\tilde{L}})_{ij}^2 &= \frac{3\Lambda^2}{160\pi^4} [\delta_{ij} \pi^2 (\alpha_1^2 + 5\alpha_2^2)], \\
 (m_{\tilde{E}})_{ij}^2 &= \frac{\Lambda^2}{640\pi^4} \left\{ \delta_{ij} 48\pi^2 \alpha_1^2 + \delta_{i3}\delta_{j3} |h_3|^2 [35|h_3|^2 - 12\pi(3\alpha_1 + 5\alpha_2)] \right\},
 \end{aligned}$$

$$\begin{aligned}
m_{H_u}^2 &= \frac{3\Lambda^2}{160\pi^4} \left[\pi^2(\alpha_1^2 + 5\alpha_2^2) - \frac{5}{8}|h_3|^2|y_t|^2 - \frac{5}{6}\lambda^2|h_3|^2 \right], \\
m_{H_d}^2 &= \frac{3\Lambda^2}{160\pi^4} \left\{ \pi^2(\alpha_1^2 + 5\alpha_2^2) + \frac{1}{24}|h_3|^2 [140|h_3|^2 + 15|y_t|^2 - 16\pi(4\alpha_1 + 15\alpha_2 + 20\alpha_3)] \right\}, \\
A_t &= -\frac{\Lambda}{16\pi^2}|h_3|^2, \\
A_\lambda &= -\frac{4|h_3|^2}{16\pi^2}\Lambda, \\
m_S^2 &= -\frac{\lambda^2|h_3|^2}{32\pi^4}\Lambda^2,
\end{aligned} \tag{A.1}$$

According to the SLHA2 convention [58] that we employ here, A_t is related to the “up” trilinear coupling $(T_u)_{33}$ as $A_t = (T_u)_{33}/y_t$.⁵ Note also that we choose $\Lambda > 0$, so that both A_λ and m_S^2 are bound to assume exclusively negative values.

At the leading order (one loop) gaugino masses at M_Y are directly related to the gauge coupling constants and given by

$$M_i = \frac{\Lambda\alpha_i}{4\pi} \quad \text{for } i = 1, 2, 3. \tag{A.2}$$

As was shown in the numerical analysis of section 3, some of the soft masses become negative for some h_3 values. As an example, one can derive from eqs. (A.1) some naive bounds, where for simplicity all α ’s are set equal to $1/20$ at M_Y , $y_t \approx 0.6$, and $\tan\beta < 10$:

$$h_3 < \frac{1}{12} \quad \text{or} \quad \frac{1}{4} < h_3 < 1.3. \tag{A.3}$$

However, the above values are just indicative. The full numerical bounds are shown in section 3.

B Sources of effective interactions below the messenger scale

We will discuss here corrections to the dynamics of S due to various processes that might take place in a UV completion of our PQ NMMSM.⁶ We base our arguments on certain F-theoretic constructions. As explained, e.g., in refs. [4, 5], chiral matter originates from two D7-branes intersecting along a 2-dimensional Riemann surface; matter interactions come from the intersection of three D7-branes at one point, which results in the intersection of three matter Riemann surfaces at this point. These intersections are generic, in the sense that they naturally emerge in the geometry of the string compactification. Thus, at the compactification scale the only natural matter couplings are cubic, and for this reason we set the mass term XS to zero in section 2.2. The same argument also suggests that all natural couplings in the superpotential should be of the order of 1. The simple picture just described is generally amended in the presence of family effects [7], instantons, which we

⁵Recall that intergenerational up trilinear couplings enter the scalar potential, V , as $V \supset -H_u\tilde{Q}_i(T_u)_{ij}(\tilde{u}_R)_j$.

⁶For a different approach see, e.g., the analysis of ref. [59].

discuss below, and possibly other effects that we do not discuss here and are difficult to estimate without a detailed knowledge of the full F-theory model.

We include in the analysis all important terms in the spurion X , whose vev gives a mass to the messengers and breaks SUSY. Below the messenger scale, $M_Y \equiv \langle X \rangle$, the spurion will be a nondynamical field, i.e., we set $X \rightarrow \langle X \rangle + \theta^2 F_X$. F_X will be the primary source of SUSY breaking, which means that F -terms of other fields must be much smaller ($\xi_F \ll F_X$ in what follows). Note that $\langle X \rangle$ breaks also $U(1)_{PQ}$. This means that at low energies there appear new effective $U(1)_{PQ}$ breaking interaction terms.

The contributions that might be relevant below M_Y can have various sources. For the low-energy dynamics the most important will be terms with powers of the spurion superfield X , because X receives a large vev. As usual, operators of dimension 5 and higher will be suppressed by a large mass scale of the order of M_{GUT} or even M_{Pl} .

Giudice-Masiero term. Besides the superpotential term (2.4), the only cubic couplings of S , X allowed by $U(1)_{PQ}$ is in the Kähler potential:

$$\delta K = \lambda_\mu \frac{X^\dagger}{M_{GUT}} H_u H_d + \text{h.c.}, \quad (\text{B.1})$$

where λ_μ is a complex constant difficult to estimate [60].

The Kähler potential δK can generate an additional μ term in the superpotential when the spurion X gets its vev, like in the Giudice-Masiero [41] mechanism: $\mu_{GM} = \lambda_\mu F_X^*/M_{GUT}$. However, one can either choose $\lambda_\mu = 0$, or perform a redefinition of the field, $S \rightarrow S - \mu_{GM}/\lambda$, which makes μ_{GM} disappear from the superpotential, and at the same time generates corrections to the tadpoles, $\delta\xi_F$ and $\delta\xi_S$, and a $B\mu$ term, m_3^3 , of the form:

$$\begin{aligned} \delta\xi_F &= -\frac{\lambda_\mu}{\lambda} \mu' \Lambda x, \\ \delta\xi_S &= -\frac{\lambda_\mu}{\lambda} m_S'^2 \Lambda x - \frac{\lambda_\mu^*}{\lambda^*} m_S^2 \Lambda x, \\ m_3^2 &= -\lambda_\mu A_\lambda \Lambda x, \end{aligned} \quad (\text{B.2})$$

where μ' , $m_S'^2$, m_S^2 , and A_λ are given in eqs. (2.9) and (A.1).

Note that in both cases the only origin of the μ -term remains the vev of the singlet, $s = \langle S \rangle$, so that $\mu_{\text{eff}} = \lambda s$.

Instantons. In stringy models there are several types of instantons [61, 62]. An instanton action, $S_{\mathcal{I}}$, depends on various moduli fields, which generally belong to two main categories, “twisted” and “untwisted”. Twisted instantons can transform by a shift under some abelian gauge symmetry, which in our case means that our $U(1)_{PQ}$ effectively gives a charge to $e^{-S_{\mathcal{I}}}$. When the moduli are set to some fixed value, $e^{-S_{\mathcal{I}}}$ becomes a numerical factor, which we denote here as $I_{q,n}$. In this case q is the $U(1)_{PQ}$ charge carried by the instanton and n indicates how many fields are associated with it, as shown below. Some of the instanton contributions are expected to vanish, while the ones that are present are expected to be strongly suppressed, $I_{q,n} \ll 1$.

Instanton effects allow one to generate new terms in the superpotential (corrections to the Kähler potential are negligible):

$$\delta W_{\mathcal{I}} = M_{\text{Pl}}^2 I_{-1,1} S + M_{\text{Pl}} (I_{0,2} X S + I_{-2,2} S^2) + I_{1,3} X^2 S + I_{-1,3} X S^2 + I_{-3,3} S^3 + \dots \quad (\text{B.3})$$

where M_{Pl} is the reduced Planck mass and the ellipsis denotes higher powers of the fields, and we have here suppressed all terms depending on X solely.

As one can see, $\kappa \approx 0$, whereas other possible contributions might be important due to the large values of M_{Pl} , $\langle X \rangle$, and F_X . The surviving terms are

$$\begin{aligned} \delta W_{\mathcal{I}} &\supset (M_{\text{Pl}}^2 I_{-1,1} + M_{\text{Pl}} \langle X \rangle I_{0,2} + I_{1,3} \langle X \rangle^2) S + (M_{\text{Pl}} I_{-2,2} + I_{-1,3} \langle X \rangle) S^2 \\ &= M_{\text{Pl}}^2 (I_{-1,1} + \eta I_{0,2} + \eta^2 I_{1,3}) S + M_{\text{Pl}} (I_{-2,2} + \eta I_{-1,3}) S^2, \end{aligned} \quad (\text{B.4})$$

$$\delta L_{\mathcal{I}} = F_X M_{\text{Pl}} (I_{0,2} + 2\eta I_{1,3}) S + I_{-1,3} F_X S^2, \quad (\text{B.5})$$

where $\eta = \langle X \rangle / M_{\text{Pl}} \ll 1$.

From eq. (B.4) follows that if all $I_{q,n}$ are approximately of the same order of magnitude the most important contributions are those characterized by the lowest $\text{U}(1)_{\text{PQ}}$ charges, q . However, it is not uncommon for the dynamics of the UV stringy theory to generate selection rules that can forbid certain terms. If, for example, $I_{q \leq 0, n} = 0$ due to the UV dynamics, one is left only with

$$\begin{aligned} \delta W_{\mathcal{I}} &= \langle X \rangle^2 I_{1,3} S, \\ \delta L_{\mathcal{I}} &= 2F_X \langle X \rangle I_{1,3} S. \end{aligned} \quad (\text{B.6})$$

In our study we always make this assumption, as it will be beneficial to reducing the fine tuning of the model.

Exchange of a heavy chiral $\text{U}(1)_{\text{PQ}}$ neutral superfield. In general, string theory constructions imply the presence of some $\text{U}(1)_{\text{PQ}}$ heavy chiral neutral superfields at the GUT scale that can be integrated out.

The simplest superpotential coupling with one heavy chiral state Ψ reads: $W \supset \lambda_{\Psi} X S \Psi + \frac{1}{2} M_{\Psi} \Psi^2$. Integrating out Ψ gives

$$\delta W_{\Psi} = -\frac{\lambda_{\Psi}^2}{2M_{\Psi}} (X S)^2, \quad \delta K_{\Psi} = \frac{|\lambda_{\Psi}|^2}{M_{\Psi}^2} (X S)^{\dagger} (X S), \quad (\text{B.7})$$

which after SUSY breaking yields

$$\delta W_{\Psi} = -\frac{\lambda_{\Psi}^2}{2M_{\Psi}} \langle X \rangle^2 S^2 = \frac{1}{2} \mu' S^2, \quad (\text{B.8})$$

and

$$\delta L_{W,\Psi} = \frac{\lambda_{\Psi}^2}{M_{\Psi}} F_X \langle X \rangle S^2 + \text{h. c.} = -\frac{1}{2} m_S'^2 S^2 + \text{h. c.} \quad (\text{B.9})$$

from the superpotential and

$$\delta L_{K,\Psi} = \frac{|\lambda_{\Psi}|^2}{M_{\Psi}^2} |F_X|^2 |S|^2 = -\delta m_S^2 |S|^2 \quad (\text{B.10})$$

from the Kähler potential (see section 2.3).

As was explained in section 2.3, we expect $M_{\Psi} \approx M_{\text{GUT}}$ and $\lambda_{\Psi} \approx 1$ if nonvanishing.

Exchange of a $U(1)_{PQ}$ heavy gauge boson. Exchange of a heavy gauge boson V associated with the breaking of $U(1)_{PQ}$ can also contribute to the scalar Lagrangian:

$$\delta K_V = -\frac{g_{PQ}^2 q_X q_j}{M_V^2} (X^\dagger X) (\Phi_j^\dagger \Phi_j) \Rightarrow \delta L_V = -\frac{g_{PQ}^2 q_X q_j}{M_V^2} |F_X|^2 \Phi_j^\dagger \Phi_j \quad \text{for all } j, \quad (\text{B.11})$$

where Φ_j are the $U(1)_{PQ}$ charged fields, q_j are their charges, g_{PQ} is a generic coupling constant, and $M_V \approx M_{\text{GUT}}$. Equation (B.11) implies that all the soft masses squared \tilde{m}_j^2 will receive an additional correction of the order of $g_{PQ}^2 q_X q_j \Lambda^2 x^2$.

Other contributions. There are more terms preserving $U(1)_{PQ}$ which might renormalize the Kähler potential as, for example, $\delta K = \frac{1}{M^2} X^\dagger X X S + \text{c.c.}$ With $M \approx M_{\text{GUT}}$ they are negligible, so that we will not try to pinpoint their sources here.

Leading supergravity corrections. Supergravity corrections [63] for $W = W_0 + F_X X + \xi_F S + \frac{1}{2} \mu' S^2$ (with $\xi_F \ll F_X$) and for the canonical Kähler potential subject to the condition of vanishing cosmological constant read:

$$\delta V(S) = \left(-2 \frac{F_X^* \xi_F}{\sqrt{3} M_{\text{Pl}}} S - \frac{F_X^* \mu'}{\sqrt{3} M_{\text{Pl}}} S^2 + \text{c.c.} \right) + 4 \frac{|F_X|^2}{3 M_{\text{Pl}}^2} |S|^2 + \dots \quad (\text{B.12})$$

They are also negligible.

In summary, when expressed in terms of $\Lambda = F_X/M_Y$ and $x = M_Y/M_{\text{GUT}}$, the full corrections to the superpotential and soft SUSY breaking terms are the following:

$$\begin{aligned} \delta m_i^2 &= g_{PQ}^2 q_X q_i |\Lambda|^2 x^2 \\ \delta m_S^2 &= -|\lambda_\Psi|^2 |\Lambda|^2 x^2 + g_{PQ}^2 q_X q_S |\Lambda|^2 x^2 \\ \mu' &= -\lambda_\Psi^2 M_{\text{GUT}} x^2, \\ m_S'^2 &= 2\lambda_\Psi^2 \Lambda M_{\text{GUT}} x^2 = -2\mu' \Lambda, \\ m_3^2 &= -\lambda_\mu A_\lambda \Lambda x, \\ \xi_F &= I_{1,3} M_{\text{GUT}}^2 x^2 + \frac{\lambda_\mu \lambda_\Psi^2}{\lambda} M_{\text{GUT}} \Lambda x^3, \\ \xi_S &= -2I_{1,3} \Lambda M_{\text{GUT}}^2 x^2 - \frac{2\lambda_\mu \lambda_\Psi^2}{\lambda} \Lambda^2 x^3 M_{\text{GUT}} + \frac{\lambda_\mu^* \lambda_\Psi^2}{\lambda^*} \Lambda^3 x^3 - \frac{\lambda_\mu^*}{\lambda^*} m_S^2 \Lambda x, \end{aligned} \quad (\text{B.13})$$

where in the last equation of (B.13) m_S^2 is the term calculated in appendix A.

Since typical values of Λ imply that $\Lambda x \ll M_{\text{GUT}}$, in our study we assume $\lambda_\mu = 0$ without loss of generality. Moreover, $\Lambda^2 x^2 \ll M_{\text{SUSY}}^2$ so that we can neglect the g_{PQ} corrections to the soft masses. Note that when $\lambda_\mu = 0$ and $g_{PQ} = 0$, eqs. (B.13) reduce to the form given in eqs. (2.9).

C Estimates of constants

In this appendix we estimate the order of magnitude of different coefficients appearing in the Lagrangian. For simplicity in what follows all coefficients are assumed to be real. We consider constraints that come from the tree-level vacuum equations of motion (e.o.m.), and those that follow from the stability of the physical vacuum.

Let us recall that $\kappa = 0$, $A_\kappa = 0$, and we are interested in small $\tan \beta$ values. Moreover, we assume that all the GMSB soft masses given in appendix A are of the order of $M_{\text{SUSY}} \ll \Lambda$. We also assume that no accidental cancellation takes place between different terms. We only consider terms in leading powers of v , and do not explicitly differentiate between constants of the order of a few.

The vacuum e.o.m. are given by:

$$\sin 2\beta - \frac{2(\lambda s A_\lambda + \hat{m}_3^2)}{2\lambda^2 s^2 + \lambda^2 v^2 + m_{H_d}^2 + m_{H_u}^2} = 0, \quad (\text{C.1})$$

$$(\lambda^2 - g^2) v^2 + \tan 2\beta (-m_{H_d}^2 + m_{H_u}^2) - \frac{2}{\tan 2\beta} (\lambda s A_\lambda + \hat{m}_3^2) = 0, \quad (\text{C.2})$$

$$s(m_S^2 + m_S'^2 + \mu'^2 + \lambda^2 v^2) + \xi_S + \xi_F \mu' - \lambda v^2 \frac{\sin 2\beta}{2} (A_\lambda + \mu') = 0, \quad (\text{C.3})$$

where $g^2 = (g_1^2 + g_2^2)/2$ and $\hat{m}_3^2 = m_3^2 + \lambda(\mu' s + \xi_F)$. Short inspection of the e.o.m. reveals that for $\tan \beta$ equals a few, s is of the order of the soft SUSY masses, $s \sim M_{\text{SUSY}}$. Thus, since $\sin 2\beta \sim 1$ one also finds $\hat{m}_3^2 \sim \mu' s + \xi_F \lesssim M_{\text{SUSY}}$.

On the other hand, the requirement of tree-level stability in the scalar sector yields⁷

$$[-2s\lambda + (A_\lambda + \mu') \sin 2\beta]^2 < -\frac{(\xi_S + \xi_F \mu')}{s}, \quad (\text{C.4})$$

which implies

$$-(\xi_S + \xi_F \mu')/s \gtrsim \max(\mu'^2, M_{\text{SUSY}}^2). \quad (\text{C.5})$$

By using eq. (C.3) one can derive

$$(m_S^2 + m_S'^2 + \mu'^2) \gtrsim \max(\mu'^2, M_{\text{SUSY}}^2), \quad (\text{C.6})$$

which is trivially satisfied when $m_S'^2 > 0$ and $m_S^2 < 0$, as is the case at hand (see appendix A). On the other hand, requiring tree-level stability of the pseudo-scalar masses, whose expressions can also be found in [40], yields an additional constraint:

$$-2m_S'^2 - \frac{(\xi_S + \xi_F \mu')}{s} > 0. \quad (\text{C.7})$$

Thus eq. (C.3) also implies $(m_S^2 - m_S'^2 + \mu'^2) > 0$, which in turns implies $m_S'^2 < \mu'^2$. Assuming a relation $m_S'^2 = -c\mu'\Lambda$, with $c > 0$, just like in eq. (2.9), one gets

$$-\mu' \gtrsim c\Lambda. \quad (\text{C.8})$$

⁷We analyze here the diagonal minors of the scalar mass matrix, which can be explicitly found, e.g., in ref. [40].

These arguments show that for small $\tan \beta$, which is the case of interest here, one can get reasonable physics only when the mass scale associated with ξ_S , ξ_F , $m_S'^2$, and μ' is much larger than M_{SUSY} .

By reinserting eq. (C.8) back into eqs. (C.1)–(C.3) one can finally infer that $s + \xi_F/\mu' \approx 0$ and $s + \xi_S/m_S'^2 \approx 0$ should simultaneously hold, up to terms that are much smaller than M_{SUSY} . Thus, one can derive the relation (2.11),

$$\frac{\xi_S}{\xi_F} = \frac{m_S'^2}{\mu'}, \quad (\text{C.9})$$

which must hold at the EW scale.

To summarize, we present all the coefficients for which the hierarchy $M_{\text{SUSY}} \ll \Lambda \lesssim |\mu'|$ holds in terms of M_{SUSY} , Λ , and $|\mu'|$:

$$\xi_F \approx -M_{\text{SUSY}}\mu', \quad \xi_S \approx M_{\text{SUSY}}\Lambda\mu', \quad m_S'^2 \approx -\Lambda\mu' \quad (\text{C.10})$$

Our numerical analysis confirms these predictions. Note that $\mu' < 0$ implies $\xi_F > 0$. The sign of ξ_F (as well as that of λ) can be always be chosen positive by rescaling the S and, e.g., H_u superfields.

As we claimed in section 2.3, the relation (C.9) is set at the M_Y scale when appropriate instanton corrections are chosen. More importantly for the fine tuning calculation, however, eq. (C.9) is approximately RG invariant, so that it continues to hold at different scales. We prove this by writing down the one-loop leading terms in the RG running:

$$\begin{aligned} \delta \log \xi_F &= \lambda^2, & \delta \log \mu' &= 2\lambda^2 \\ \delta \log \xi_S &\approx \lambda^2(1 + 2A_\lambda \xi_F/\xi_S), & \delta \log m_S'^2 &= 2\lambda^2(1 + 2A_\lambda \mu'/m_S'^2), \end{aligned}$$

where we have used the estimates in (C.10) and the simplified notation $\delta = 16\pi^2 \frac{d}{dt}$. The terms in parentheses are approximately 1 so that

$$\delta \log \left(\frac{\xi_S}{\xi_F} \right) \approx \delta \log \left(\frac{m_S'^2}{\mu'} \right) \approx 0, \quad (\text{C.11})$$

which leads to eq. (C.9).

D Tree level Higgs mass in the PQ NMSSM

Tree-level masses of the three CP-even Higgs bosons in the PQ NMSSM can be calculated by diagonalizing the mass matrix explicitly given, e.g., in ref. [40]. We give here approximate formulas for the lightest eigenvalue.

We assume the following hierarchy of the mass matrix eigenvalues: $m_{h_1} \ll m_{h_2} \ll m_{h_3}$. One can thus show that

$$m_{h_1, \text{tree}}^2 \approx v^2 (g^2 \cos^2 2\beta + \lambda^2 \sin^2 2\beta) + \frac{sv^2 \lambda^2 (2s\lambda - A_\lambda \sin 2\beta - \mu' \sin 2\beta)^2}{\xi_S + \xi_F \mu'}. \quad (\text{D.1})$$

Since μ' is much larger than the GMSB-generated soft terms given in eqs. (A.1), one can further reduce eq. (D.1) to

$$m_{h_1, \text{tree}}^2 \approx M_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta \left(1 + \frac{\mu'^2}{(\xi_S + \xi_F \mu')/s} \right). \quad (\text{D.2})$$

Note that in the model presented in this paper $(\xi_S + \xi_F \mu')/s < 0$.

One can schematically separate eq. (D.2) into the MSSM and λ -dependent parts: $m_{h_1, \text{tree}}^2 = M_Z^2 \cos^2 2\beta + \delta m_{h_1, \text{tree}}^2$. One should recall from appendix C that $\xi_F \approx -\mu' s$, so that we get

$$\delta m_{h_1, \text{tree}}^2 = \lambda^2 v^2 \sin^2 2\beta \left(1 - \frac{1}{1 + \frac{\xi_S}{\xi_F \mu'}} \right) \approx \lambda^2 v^2 \sin^2 2\beta \cdot \frac{\xi_S}{\xi_F \mu'}, \quad (\text{D.3})$$

which was used in the discussion of section 3. As was mentioned over there, when $\xi_S \ll \xi_F \mu'$ one gets $\delta m_{h_1, \text{tree}}^2 \approx 0$, even for large values of $\lambda \gtrsim 0.7$, which is the case presented in BP2 of table 1.

Recall, finally, from appendices B and C that $-\xi_S = 2\Lambda \xi_F$, and $2\Lambda \lesssim -\mu'$, which implies that in our model $\epsilon = \xi_S/\xi_F \mu' \lesssim 1$. As we discussed in section 3, we found no points for which $m_{h_1, \text{tree}}^2 > M_Z^2$, so that large radiative corrections to the Higgs mass are always necessary to obtain $m_{h_1} \approx 125 \text{ GeV}$.

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References

- [1] C.D. Froggatt and H.B. Nielsen, *Hierarchy of quark masses, Cabibbo angles and CP-violation*, *Nucl. Phys. B* **147** (1979) 277 [[INSPIRE](#)].
- [2] C. Vafa, *Evidence for F-theory*, *Nucl. Phys. B* **469** (1996) 403 [[hep-th/9602022](#)] [[INSPIRE](#)].
- [3] R. Donagi and M. Wijnholt, *Model building with F-theory*, *Adv. Theor. Math. Phys.* **15** (2011) 1237 [[arXiv:0802.2969](#)] [[INSPIRE](#)].
- [4] C. Beasley, J.J. Heckman and C. Vafa, *GUTs and exceptional branes in F-theory — I*, *JHEP* **01** (2009) 058 [[arXiv:0802.3391](#)] [[INSPIRE](#)].
- [5] C. Beasley, J.J. Heckman and C. Vafa, *GUTs and exceptional branes in F-theory — II: experimental predictions*, *JHEP* **01** (2009) 059 [[arXiv:0806.0102](#)] [[INSPIRE](#)].
- [6] J.J. Heckman, A. Tavanfar and C. Vafa, *The point of E_8 in F-theory GUTs*, *JHEP* **08** (2010) 040 [[arXiv:0906.0581](#)] [[INSPIRE](#)].
- [7] S. Cecotti, M.C.N. Cheng, J.J. Heckman and C. Vafa, *Yukawa couplings in F-theory and non-commutative geometry*, [arXiv:0910.0477](#) [[INSPIRE](#)].
- [8] J.J. Heckman, *Particle physics implications of F-theory*, *Ann. Rev. Nucl. Part. Sci.* **60** (2010) 237 [[arXiv:1001.0577](#)] [[INSPIRE](#)].
- [9] M. Dine, Y. Nir and Y. Shirman, *Variations on minimal gauge mediated supersymmetry breaking*, *Phys. Rev. D* **55** (1997) 1501 [[hep-ph/9607397](#)] [[INSPIRE](#)].

- [10] G.F. Giudice and R. Rattazzi, *Extracting supersymmetry breaking effects from wave function renormalization*, *Nucl. Phys. B* **511** (1998) 25 [[hep-ph/9706540](#)] [[INSPIRE](#)].
- [11] Z. Chacko and E. Ponton, *Yukawa deflected gauge mediation*, *Phys. Rev. D* **66** (2002) 095004 [[hep-ph/0112190](#)] [[INSPIRE](#)].
- [12] Z. Chacko, E. Katz and E. Perazzi, *Yukawa deflected gauge mediation in four dimensions*, *Phys. Rev. D* **66** (2002) 095012 [[hep-ph/0203080](#)] [[INSPIRE](#)].
- [13] M. Dine and W. Fischler, *A phenomenological model of particle physics based on supersymmetry*, *Phys. Lett. B* **110** (1982) 227 [[INSPIRE](#)].
- [14] C.R. Nappi and B.A. Ovrut, *Supersymmetric extension of the $SU(3) \times SU(2) \times U(1)$ model*, *Phys. Lett. B* **113** (1982) 175 [[INSPIRE](#)].
- [15] L. Álvarez-Gaumé, M. Claudson and M.B. Wise, *Low-energy supersymmetry*, *Nucl. Phys. B* **207** (1982) 96 [[INSPIRE](#)].
- [16] M. Dine and A.E. Nelson, *Dynamical supersymmetry breaking at low-energies*, *Phys. Rev. D* **48** (1993) 1277 [[hep-ph/9303230](#)] [[INSPIRE](#)].
- [17] M. Dine, A.E. Nelson and Y. Shirman, *Low-energy dynamical supersymmetry breaking simplified*, *Phys. Rev. D* **51** (1995) 1362 [[hep-ph/9408384](#)] [[INSPIRE](#)].
- [18] M. Dine, A.E. Nelson, Y. Nir and Y. Shirman, *New tools for low-energy dynamical supersymmetry breaking*, *Phys. Rev. D* **53** (1996) 2658 [[hep-ph/9507378](#)] [[INSPIRE](#)].
- [19] G.F. Giudice and R. Rattazzi, *Theories with gauge mediated supersymmetry breaking*, *Phys. Rept.* **322** (1999) 419 [[hep-ph/9801271](#)] [[INSPIRE](#)].
- [20] J. Pawełczyk, *A model of Yukawa couplings with matter-messenger unification*, [arXiv:1305.5162](#) [[INSPIRE](#)].
- [21] T. Jelinski and J. Pawełczyk, *Masses and FCNC in flavoured GMSB scheme*, [arXiv:1406.4001](#) [[INSPIRE](#)].
- [22] P. Fayet, *A gauge theory of weak and electromagnetic interactions with spontaneous parity breaking*, *Nucl. Phys. B* **78** (1974) 14 [[INSPIRE](#)].
- [23] P. Fayet, *Supergauge invariant extension of the Higgs mechanism and a model for the electron and its neutrino*, *Nucl. Phys. B* **90** (1975) 104 [[INSPIRE](#)].
- [24] P. Fayet, *Supersymmetry and weak, electromagnetic and strong interactions*, *Phys. Lett. B* **64** (1976) 159 [[INSPIRE](#)].
- [25] L.J. Hall and T. Watari, *Electroweak supersymmetry with an approximate $U(1)_{PQ}$* , *Phys. Rev. D* **70** (2004) 115001 [[hep-ph/0405109](#)] [[INSPIRE](#)].
- [26] B. Feldstein, L.J. Hall and T. Watari, *Simultaneous solutions of the strong CP and μ problems*, *Phys. Lett. B* **607** (2005) 155 [[hep-ph/0411013](#)] [[INSPIRE](#)].
- [27] R. Barbieri, L.J. Hall, A.Y. Papaioannou, D. Pappadopulo and V.S. Rychkov, *An alternative NMSSM phenomenology with manifest perturbative unification*, *JHEP* **03** (2008) 005 [[arXiv:0712.2903](#)] [[INSPIRE](#)].
- [28] T. Gherghetta, B. von Harling, A.D. Medina and M.A. Schmidt, *The scale-invariant NMSSM and the 126 GeV Higgs boson*, *JHEP* **02** (2013) 032 [[arXiv:1212.5243](#)] [[INSPIRE](#)].
- [29] M.B. Green and J.H. Schwarz, *Anomaly cancellation in supersymmetric $D = 10$ gauge theory and superstring theory*, *Phys. Lett. B* **149** (1984) 117 [[INSPIRE](#)].

- [30] S. Ferrara, D.V. Nanopoulos and C.A. Savoy, *Hierarchical supergravity induced $SU(2) \times U(1)$ breaking in $SU(5)$ GUTs*, *Phys. Lett. B* **123** (1983) 214 [INSPIRE].
- [31] J. Polchinski and L. Susskind, *Breaking of supersymmetry at intermediate-energy*, *Phys. Rev. D* **26** (1982) 3661 [INSPIRE].
- [32] H.P. Nilles, M. Srednicki and D. Wyler, *Constraints on the stability of mass hierarchies in supergravity*, *Phys. Lett. B* **124** (1983) 337 [INSPIRE].
- [33] A.B. Lahanas, *Light singlet, gauge hierarchy and supergravity*, *Phys. Lett. B* **124** (1983) 341 [INSPIRE].
- [34] U. Ellwanger, *Nonrenormalizable interactions from supergravity, quantum corrections and effective low-energy theories*, *Phys. Lett. B* **133** (1983) 187 [INSPIRE].
- [35] J. Bagger and E. Poppitz, *Destabilizing divergences in supergravity coupled supersymmetric theories*, *Phys. Rev. Lett.* **71** (1993) 2380 [hep-ph/9307317] [INSPIRE].
- [36] V. Jain, *On destabilizing divergencies in supergravity models*, *Phys. Lett. B* **351** (1995) 481 [hep-ph/9407382] [INSPIRE].
- [37] J. Bagger, E. Poppitz and L. Randall, *Destabilizing divergences in supergravity theories at two loops*, *Nucl. Phys. B* **455** (1995) 59 [hep-ph/9505244] [INSPIRE].
- [38] U. Ellwanger, C.C. Jean-Louis and A.M. Teixeira, *Phenomenology of the general NMSSM with gauge mediated supersymmetry breaking*, *JHEP* **05** (2008) 044 [arXiv:0803.2962] [INSPIRE].
- [39] J. Pawelczyk, *F-theory inspired GUTs with extra charged matter*, *Phys. Lett. B* **697** (2011) 75 [arXiv:1008.2254] [INSPIRE].
- [40] U. Ellwanger, C. Hugonie and A.M. Teixeira, *The next-to-minimal supersymmetric standard model*, *Phys. Rept.* **496** (2010) 1 [arXiv:0910.1785] [INSPIRE].
- [41] G.F. Giudice and A. Masiero, *A natural solution to the μ problem in supergravity theories*, *Phys. Lett. B* **206** (1988) 480 [INSPIRE].
- [42] CMS collaboration, *Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC*, *Phys. Lett. B* **716** (2012) 30 [arXiv:1207.7235] [INSPIRE].
- [43] ATLAS collaboration, *Observation of a new particle in the search for the standard model Higgs boson with the ATLAS detector at the LHC*, *Phys. Lett. B* **716** (2012) 1 [arXiv:1207.7214] [INSPIRE].
- [44] ATLAS collaboration, *Search for squarks and gluinos with the ATLAS detector in final states with jets and missing transverse momentum using $\sqrt{s} = 8$ TeV proton–proton collision data*, *JHEP* **09** (2014) 176 [arXiv:1405.7875] [INSPIRE].
- [45] ATLAS collaboration, *Search for photonic signatures of gauge-mediated supersymmetry in 8 TeV pp collisions with the ATLAS detector*, *Phys. Rev. D* **92** (2015) 072001 [arXiv:1507.05493] [INSPIRE].
- [46] CMS collaboration, *Searches for supersymmetry using the M_{T2} variable in hadronic events produced in pp collisions at 8 TeV*, *JHEP* **05** (2015) 078 [arXiv:1502.04358] [INSPIRE].
- [47] CMS collaboration, *Searches for long-lived charged particles in pp collisions at $\sqrt{s} = 7$ and 8 TeV*, *JHEP* **07** (2013) 122 [arXiv:1305.0491] [INSPIRE].
- [48] <http://www.th.u-psud.fr/NMHDECAY/nmssmtools.html>.

- [49] F. Feroz, M.P. Hobson and M. Bridges, *MultiNest: an efficient and robust Bayesian inference tool for cosmology and particle physics*, *Mon. Not. Roy. Astron. Soc.* **398** (2009) 1601 [[arXiv:0809.3437](#)] [[INSPIRE](#)].
- [50] PARTICLE DATA GROUP collaboration, K.A. Olive et al., *Review of particle physics*, *Chin. Phys. C* **38** (2014) 090001 [[INSPIRE](#)].
- [51] F. Staub et al., *Higgs mass predictions of public NMSSM spectrum generators*, [arXiv:1507.05093](#) [[INSPIRE](#)].
- [52] R. Barbieri, L.J. Hall, Y. Nomura and V.S. Rychkov, *Supersymmetry without a light Higgs boson*, *Phys. Rev. D* **75** (2007) 035007 [[hep-ph/0607332](#)] [[INSPIRE](#)].
- [53] ATLAS collaboration, *Search for supersymmetry at the high luminosity LHC with the ATLAS experiment*, *ATL-PHYS-PUB-2014-010* (2014).
- [54] ATLAS collaboration, *Physics at a high-luminosity LHC with ATLAS*, *ATL-PHYS-PUB-2012-001* (2012).
- [55] J.R. Ellis, K. Enqvist, D.V. Nanopoulos and F. Zwirner, *Observables in low-energy superstring models*, *Mod. Phys. Lett. A* **1** (1986) 57 [[INSPIRE](#)].
- [56] R. Barbieri and G.F. Giudice, *Upper bounds on supersymmetric particle masses*, *Nucl. Phys. B* **306** (1988) 63 [[INSPIRE](#)].
- [57] J.A. Evans and D. Shih, *Surveying extended GMSB models with $m_h = 125$ GeV*, *JHEP* **08** (2013) 093 [[arXiv:1303.0228](#)] [[INSPIRE](#)].
- [58] B.C. Allanach et al., *SUSY Les Houches accord 2*, *Comput. Phys. Commun.* **180** (2009) 8 [[arXiv:0801.0045](#)] [[INSPIRE](#)].
- [59] S.H. Im and M.-S. Seo, *Peccei-Quinn invariant singlet extended SUSY with anomalous U(1) gauge symmetry*, *JHEP* **05** (2015) 063 [[arXiv:1411.4724](#)] [[INSPIRE](#)].
- [60] J.J. Heckman and C. Vafa, *F-theory, GUTs and the weak scale*, *JHEP* **09** (2009) 079 [[arXiv:0809.1098](#)] [[INSPIRE](#)].
- [61] E. Witten, *Nonperturbative superpotentials in string theory*, *Nucl. Phys. B* **474** (1996) 343 [[hep-th/9604030](#)] [[INSPIRE](#)].
- [62] M.R. Douglas and G.W. Moore, *D-branes, quivers and ALE instantons*, [hep-th/9603167](#) [[INSPIRE](#)].
- [63] P. Binetruy, G. Dvali, R. Kallosh and A. Van Proeyen, *Fayet-Iliopoulos terms in supergravity and cosmology*, *Class. Quant. Grav.* **21** (2004) 3137 [[hep-th/0402046](#)] [[INSPIRE](#)].